Amendments to the Claims:

This listing of claims will replace all prior versions and listings of claims in the application.

Listing of Claims:

- 1 18. (Cancelled)
- 19. (New) A computer implemented process comprising:

obtaining a set of one or more private values $Q_1,Q_2,...,Q_m$ and respective public values $G_1,G_2,...,G_m$, each pair of values (Q_i,G_i) verifying either the equation $G_i \cdot Q_i^{\ \nu} \equiv 1 \bmod n$ or the equation $G_i \equiv Q_i^{\ \nu} \bmod n$, wherein m is an integer greater than or equal to 1, i is an integer between 1 and m, and wherein n is a public integer equal to the product of f private prime factors designated by $p_1,...,p_f$, at least two of these prime factors being different from each other, wherein f is an integer greater than 1, and wherein ν is a public exponent such that $\nu = 2^k$, and wherein k is a security parameter having an integer value greater than 1, and wherein each public value G_i (for i = 1,...,m) is such that $G_i \equiv g_i^{\ 2} \bmod n$, wherein g_i (for i = 1,...,m) is a base number having an integer value greater than 1 and smaller than each of the prime factors $p_1,...,p_f$, and g_i is a non-quadratic residue of the body of integers modulo n; and

using at least the private values $Q_1, Q_2, ..., Q_m$ in an authentication or in a signature method.

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20. (New) The computer implemented process according to claim 19, further comprising:

receiving a commitment R from a demonstrator, the commitment R having a value computed such that: $R = r^{\nu} \mod n$, wherein r is an integer randomly chosen by the demonstrator;

choosing m challenges $d_1, d_2, ..., d_m$ randomly;

sending the challenges $d_1, d_2, ..., d_m$ to the demonstrator;

receiving a response D from the demonstrator, the response D having a value computed such that: $D = r \times Q_1^{d_1} \times Q_2^{d_2} \times ... \times Q_m^{d_m} \mod n$; and

determining that the demonstrator is authentic if the response D has a value such that: $D^{\nu} \times G_1^{\varepsilon_1 d_1} \times G_2^{\varepsilon_2 d_2} \times ... \times G_m^{\varepsilon_m d_m} \mod n \text{ is equal to the commitment } R \text{, wherein, for } i = 1,...,m,$ $\varepsilon_i = +1 \text{ in the case } G_i \times Q_i^{\nu} = 1 \mod n \text{ and } \varepsilon_i = -1 \text{ in the case } G_i = Q_i^{\nu} \mod n.$

21. (New) The computer implemented process according to claim 19, further comprising:

receiving a commitment R from a demonstrator, the commitment R having a value computed using the Chinese remainder method from a series of commitment components R_j , the commitment components R_j having a value such that: $R_j = r_j^{\nu} \mod p_j$ for j = 1,...,f, wherein $r_1,...,r_f$ is a series of integers randomly chosen by the demonstrator;

choosing m challenges $d_1, d_2, ..., d_m$ randomly;

sending the challenges $d_1, d_2, ..., d_m$ to the demonstrator;

receiving a response D from the demonstrator, the response D being computed from a series of response components D_j using the Chinese remainder method, the response components D_j having a value such that: $D_j = r_j \times Q_{1,j}^{-d_1} \times Q_{2,j}^{-d_2} \times ... \times Q_{m,j}^{-d_m} \mod p_j$ for j = 1,...,f, wherein $Q_{i,j} = Q_i \mod p_j$ for i = 1,...,m and j = 1,...,f; and

determining that the demonstrator is authentic if the response D has a value such that: $D^{\nu} \times G_1^{\epsilon_1 d_1} \times G_2^{\epsilon_2 d_2} \times ... \times G_m^{\epsilon_m d_m} \mod n \text{ is equal to the commitment } R \text{, wherein, for } i=1,...,m,$ $\varepsilon_i = +1 \text{ in the case } G_i \times Q_i^{\nu} = 1 \mod n \text{ and } \varepsilon_i = -1 \text{ in the case } G_i = Q_i^{\nu} \mod n.$

22. (New) The computer implemented process according to claim 19, further comprising:

receiving a token T from a demonstrator, the token T having a value such that T = h(M, R), wherein h is a hash function, M is a message received from the demonstrator, and R is a commitment having a value computed such that: $R = r^{\nu} \mod n$, wherein r is an integer randomly chosen by the demonstrator;

choosing m challenges $d_1, d_2, ..., d_m$ randomly;

sending the challenges $d_1, d_2, ..., d_m$ to the demonstrator;

receiving a response D from the demonstrator, the response D having a value such that: $D = r \times Q_1^{d_1} \times Q_2^{d_2} \times ... \times Q_m^{d_m} \mod n$; and

determining that the message M is authentic if the response D has a value such that: $h\left(M, D^{\nu} \times G_{1}^{\varepsilon_{1}d_{1}} \times G_{2}^{\varepsilon_{2}d_{2}} \times ... \times G_{m}^{\varepsilon_{m}d_{m}} \mod n\right) \text{ is equal to the token } T \text{ , wherein, for } i=1,...,m\,,$ $\varepsilon_{i}=+1 \text{ in the case } G_{i} \times Q_{i}^{\nu}=1 \mod n \text{ and } \varepsilon_{i}=-1 \text{ in the case } G_{i}=Q_{i}^{\nu} \mod n\,.$

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23. (New) The computer implemented process according to claim 19, further comprising:

receiving a token T from a demonstrator, the token T having a value such that T = h(M,R), wherein h is a hash function, M is a message received from the demonstrator, and R is a commitment having a value computed out of commitment components R_j by using the Chinese remainder method, the commitment components R_j having a value such that: $R_j = r_j^{\nu} \mod p_j$ for j = 1,...,f, wherein $r_1,...,r_f$ is a series of integers randomly chosen by the demonstrator;

choosing m challenges $d_1, d_2, ..., d_m$ randomly;

sending the challenges $d_1, d_2, ..., d_m$ to the demonstrator;

receiving a response D_i from the demonstrator, the response D_i being computed from a series of response components D_j using the Chinese remainder method, the response components D_j having a value such that: $D_j = r_j \times Q_{1,j}^{-d_1} \times Q_{2,j}^{-d_2} \times ... \times Q_{m,j}^{-d_m} \mod p_j$ for j = 1,...,f, wherein $Q_{i,j} = Q_i \mod p_j$ for i = 1,...,m and j = 1,...,f; and

determining that the message M is authentic if the response D has a value such that: $h(M, D^{\nu} \times G_1^{\epsilon_1 d_1} \times G_2^{\epsilon_2 d_2} \times ... \times G_m^{\epsilon_m d_m} \mod n) \text{ is equal to the token } T \text{ , wherein, for } i = 1, ..., m,$ $\varepsilon_i = +1 \text{ in the case } G_i \times Q_i^{\nu} = 1 \mod n \text{ and } \varepsilon_i = -1 \text{ in the case } G_i = Q_i^{\nu} \mod n.$

- 24. (New) The process according to claim 20, wherein the challenges are such that $0 \le d_i \le 2^k 1$ for i = 1,...,m.
- 25. (New) A process according to claim 19 for allowing a signatory to sign a message M, the method further comprising:

choosing m integers r_i randomly, wherein i is an integer between 1 and m;

computing commitments R_i having a value such that: $R_i = r_i^{\nu} \mod n$ for i = 1,...,m;

computing a token T having a value such that $T = h(M, R_1, R_2, ..., R_m)$, wherein h is a hash function producing a binary train consisting of m bits;

identifying the bits $d_1, d_2, ..., d_m$ of the token T; and

computing responses $D_i = r_i \times Q_i^{d_i} \mod n$ for i = 1,...,m.

26. (New) The process of claim 25, further comprising:

collecting the token T and the responses D_i for i = 1,...,m; and

determining that the message M is authentic if the response D has a value such that: $h(M, D^{\nu} \times G_1^{\varepsilon_1 d_1} \times G_2^{\varepsilon_2 d_2} \times ... \times G_m^{\varepsilon_m d_m} \mod n) \text{ is equal to the token } T \text{ , wherein, for } i = 1, ..., m,$ $\varepsilon_i = +1 \text{ in the case } G_i \times Q_i^{\nu} = 1 \mod n \text{ and } \varepsilon_i = -1 \text{ in the case } G_i = Q_i^{\nu} \mod n.$

27. (New) A system used in a cryptographic process using asymmetric keys, the system comprising:

a memory storing a set of instructions; and

a processor coupled to the memory for executing the set of instructions stored in the memory, the instructions including:

obtaining a set of one or more private values $Q_1, Q_2, ..., Q_m$ and respective public values $G_1, G_2, ..., G_m$, each pair of keys (Q_i, G_i) verifying either the equation $G_i \cdot Q_i^{\nu} \equiv 1 \mod n$ or the

equation $G_i \equiv Q_i^{\ \nu} \mod n$, wherein m is an integer greater than or equal to 1, i is an integer between 1 and m, and wherein n is a public integer equal to the product of f private prime factors designated by p_1, \ldots, p_f , at least two of these prime factors being different from each other, wherein f is an integer greater than 1, and wherein v is a public exponent such that $v=2^k$, and wherein k is a security parameter having an integer value greater than 1, and wherein each public value G_i (for $i=1,\ldots,m$) is such that $G_i \equiv g_i^{\ 2} \mod n$, wherein g_i (for $i=1,\ldots,m$) is a base number having an integer value greater than 1 and smaller than each of the prime factors p_1,\ldots,p_f , and g_i is a non-quadratic residue of the body of integers modulo n; and

using at least the private values $Q_1, Q_2, ..., Q_m$ in an authentication or in a signature method.

28. (New) A computer readable medium containing computer code programmed for execution on multiple threads, the computer code comprising:

obtaining a set of one or more private values $Q_1, Q_2, ..., Q_m$ and respective public values $G_1, G_2, ..., G_m$, each pair of keys (Q_i, G_i) verifying either the equation $G_i \cdot Q_i^{\ \nu} \equiv 1 \mod n$ or the equation $G_i \equiv Q_i^{\ \nu} \mod n$, wherein m is an integer greater than or equal to 1, i is an integer between 1 and m, and wherein n is a public integer equal to the product of f private prime factors designated by $p_1, ..., p_f$, at least two of these prime factors being different from each other, wherein f is an integer greater than 1, and wherein ν is a public exponent such that $\nu = 2^k$, and wherein k is a security parameter having an integer value greater than 1, and wherein each public value G_i (for i = 1, ..., m) is such that $G_i \equiv g_i^{\ \nu} \mod n$, wherein g_i (for i = 1, ..., m) is a base number having an integer value greater than 1 and smaller than each of the prime factors $p_1, ..., p_f$, and g_i is a non-quadratic residue of the body of integers modulo n; and

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using at least the private values $Q_1, Q_2, ..., Q_m$ in an authentication or in a signature method.